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EDITION



# Essential Statistics

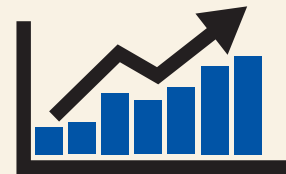
*Exploring the World through Data*

SECOND EDITION

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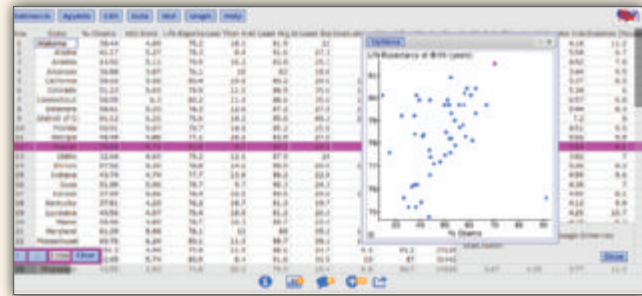


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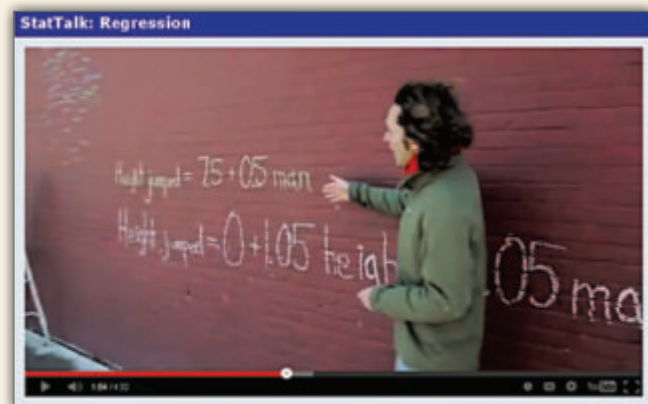


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# Essential Statistics: Exploring the World through Data

Second Edition

Global Edition

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University of California, Los Angeles

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West Valley College



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## *Dedication*

To my parents and family, my friends, and my colleagues who are also friends. Without their patience and support, this would not have been possible.

—Rob

To my teachers and students, and to my family who have helped me in many different ways.

—Colleen

To my students, colleagues, family, and friends who have helped me be a better teacher and a better person.

—Rebecca

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Colleen earned a B.A. in physics from Wellesley College, an M.A.T. in physics from Harvard University, and an M.A. in chemistry from Wellesley College. Her first exposure to statistics was with Frederick Mosteller at Harvard.

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Rebecca earned a B.A. in mathematics and psychology from the University of California, Santa Barbara, an M.S.T. in mathematics from Santa Clara University, and an Ed.D. in Educational Leadership from San Francisco State University. She has been recognized for outstanding teaching by the National Institute of Staff and Organizational Development and the California Mathematics Council of Community Colleges.

When not teaching, Rebecca is an avid reader and enjoys hiking trails with friends.

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# Preface

## About This Text

The primary focus of this text is still, as in the first edition, data. We live in a data-driven economy and, more and more, in a data-centered culture. We don't choose whether we interact with data; the choice is made for us by websites that track our browsing patterns, membership cards that track our spending habits, cars that transmit our driving patterns, and smart phones that record our most personal moments.

The silver lining of what some have called the Data Deluge is that we all have access to rich and valuable data relevant in many important fields: environment, civics, social sciences, economics, health care, entertainment. This text teaches students to learn from such data and, we hope, to become cognizant of the role of the data that appear all around them. We want students to develop a data habit of mind in which, when faced with decisions, claims, or just plain curiosity, they know to reach for an appropriate data set to answer their questions. More important, we want them to have the skills to access these data and the understanding to analyze the data critically. Clearly, we've come a long way from the "mean median mode" days of rote calculation. To survive in the modern economy requires much more than knowing how to plug numbers into a formula. Today's students must know which questions can be answered by applying which statistic, and how to get technology to compute these statistics from within complex data sets.

## What's New in the Second Edition

The second edition remains true to the goals of the first edition: to provide students with the tools they need to make sense of the world by teaching them to collect, visualize, analyze, and interpret data. With the help of several wise and careful readers and class testers, we have fine-tuned the second edition to better achieve this vision. In some sections, we have rewritten explanations or added new ones. In others, we have more substantially reordered content.

More precisely, in this new edition you will find

- Coverage of two-proportion confidence intervals in Chapters 7 and 8.
- An increase of more than 150 homework exercises in this edition, with more than 400 total new, revised, and updated exercises. We've added larger data sets to Chapters 2, 3, 4, and 9. We've also added exercises to Section 2.5 and more Chapter Review exercises throughout.
- New or updated examples in each chapter, with current topics such as views of stem cell research (Chapter 7) and online classes (Chapter 10).
- A more careful and thorough integration of technology in many examples.
- Two new case studies: Student-to-Teacher Ratios in Chapter 2 and Dodging the Question in Chapter 8.
- A more straightforward implementation of simulations to understand probability in Chapter 5.
- A more unified presentation of hypothesis testing in Chapter 8 that better joins conceptual understanding with application.
- A greater number of "Looking Back" and "Caution" marginal boxes to help direct students' studies.
- Updated technology guides to match current hardware and software.

## Approach

Our text is concept-based, as opposed to method-based. We teach useful statistical methods, but we emphasize that applying the method is secondary to understanding the concept.

In the real world, computers do most of the heavy lifting for statisticians. We therefore adopt an approach that frees the instructor from having to teach tedious procedures and leaves more time for teaching deeper understanding of concepts. Accordingly, we present formulas as an aid to understanding the concepts, rather than as the focus of study.

We believe students need to learn how to

- Determine which statistical procedures are appropriate.
- Instruct the software to carry out the procedures.
- Interpret the output.

We understand that students will probably see only one type of statistical software in class. But we believe it is useful for students to compare output from several different sources, so in some examples we ask them to read output from two or more software packages.

One of the authors (Rob Gould) served on a panel of co-authors for the first edition of the collegiate version of the American Statistical Association–endorsed *Guidelines for Assessment and Instruction in Statistics Education (GAISE)*. We firmly believe in its main goals and have adopted them in the preparation of this book.

- We emphasize understanding over rote performance of procedures.
- We use real data whenever possible.
- We encourage the use of technology both to develop conceptual understanding and to analyze data.
- We believe strongly that students learn by doing. For this reason, the homework problems offer students both practice in basic procedures and challenges to build conceptual understanding.

## Coverage

The first few chapters of this book are concept-driven and cover exploratory data analysis and inferential statistics—fundamental concepts that every introductory statistics student should learn. The last part of the book builds on that strong conceptual foundation and is more methods-based. It presents several popular statistical methods and more fully explores methods presented earlier.

Our ordering of topics is guided by the process through which students should analyze data. First, they explore and describe data, possibly deciding that graphics and numerical summaries provide sufficient insight. Then they make generalizations (inferences) about the larger world.

**Chapters 1–4: Exploratory Data Analysis.** The first four chapters cover data collection and summary. Chapter 1 introduces the important topic of data collection and compares and contrasts observational studies with controlled experiments. This chapter also teaches students how to handle raw data so that the data can be uploaded to their statistical software. Chapters 2 and 3 discuss graphical and numerical summaries of single variables based on samples. We emphasize that the purpose is not just to produce a graph or a number but, instead, to explain what those graphs and numbers say about the world. Chapter 4 introduces simple linear regression and presents it as a technique for providing graphical and numerical summaries of relationships between two numerical variables.

We feel strongly that introducing regression early in the text is beneficial in building student understanding of the applicability of statistics to real-world scenarios. After completing the chapters covering data collection and summary, students have acquired the skills and sophistication they need to describe two-variable associations and to generate informal hypotheses. Two-variable associations provide a rich context for class discussion and allow the course to move from fabricated problems (because one-variable analyses are relatively rare in the real world) to real problems that appear frequently in everyday life.

**Chapters 5–8: Inference.** These chapters teach the fundamental concepts of statistical inference. The main idea is that our data mirror the real world, but imperfectly; although our estimates are uncertain, under the right conditions we can quantify our uncertainty. Verifying that these conditions exist and understanding what happens if they are not satisfied are important themes of these chapters.

**Chapters 9–10: Methods.** Here we return to the themes covered earlier in the text and present them in a new context by introducing additional statistical methods, such as estimating population means and analyzing categorical variables. We also provide (in Section 10.3) guidance for reading scientific literature, to offer students the experience of critically examining real scientific papers.

## Organization

Our preferred order of progressing through the text is reflected in the Contents, but there are some alternative pathways as well.

**10-week Quarter.** The first eight chapters provide a full, one-quarter course in introductory statistics. If time remains, cover Sections 9.1 and 9.2 as well, so that students can solidify their understanding of confidence intervals and hypothesis tests by revisiting the topic with a new parameter.

**Proportions First.** Ask two statisticians, and you will get three opinions on whether it is best to teach means or proportions first. We have come down on the side of proportions for a variety of reasons. Proportions are much easier to find in popular news media (particularly around election time), so they can more readily be tied to students' everyday lives. Also, the mathematics and statistical theory are simpler; because there's no need to provide a separate estimate for the population standard deviation, inference is based on the Normal distribution, and no further approximations (that is, the  $t$ -distribution) are required. Hence, we can quickly get to the heart of the matter with fewer technical diversions.

The basic problem here is how to quantify the uncertainty involved in estimating a parameter and how to quantify the probability of making incorrect decisions when posing hypotheses. We cover these ideas in detail in the context of proportions. Students can then more easily learn how these same concepts are applied in the new context of means (and any other parameter they may need to estimate).

**Means First.** Conversely, many people feel that there is time for only one parameter and that this parameter should be the mean. For this alternative presentation, cover Chapters 6, 7, and 9, in that order. On this path, students learn about survey sampling and the terminology of inference (population vs. sample, parameter vs. statistic) and then tackle inference for the mean, including hypothesis testing.

To minimize the coverage of proportions, you might choose to cover Chapter 6, Section 7.1 (which treats the language and framework of statistical inference in detail), and then Chapter 9. Chapters 7 and 8 develop the concepts of statistical inference more slowly than Chapter 9, but essentially, Chapter 9 develops the same ideas in the context of the mean.

If you present Chapter 9 before Chapters 7 and 8, we recommend that you devote roughly twice as much time to Chapter 9 as you have devoted to previous chapters, because many challenging ideas are explored in this chapter. If you have already covered Chapters 7 and 8 thoroughly, Chapter 9 can be covered more quickly.


## Features

We've incorporated into this text a variety of features to aid student learning and to facilitate its use in any classroom.

### *Integrating Technology*

Modern statistics is inseparable from computers. We have worked to make this text accessible for any classroom, regardless of the level of in-class exposure to technology, while still remaining true to the demands of the analysis. We know that students sometimes do not have access to technology when doing homework, so many exercises provide output from software and ask students to interpret and critically evaluate that given output.

Using technology is important because it enables students to handle real data, and real data sets are often large and messy. The following features are designed to guide students.

- **TechTips** outline steps for performing calculations using TI-84<sup>®</sup> (including TI-84 + C<sup>®</sup>) graphing calculators, Excel<sup>®</sup>, Minitab<sup>®</sup>, and StatCrunch<sup>®</sup>. We do not want students to get stuck because they don't know how to reproduce the results we show in the text, so whenever a new method or procedure is introduced, an icon, , refers students to the TechTips section at the end of the chapter. Each set of TechTips contains at least one mini-example, so that students are not only learning to use the technology but also practicing data analysis and reinforcing ideas discussed in the text. Most of the provided TI-84 steps apply to all TI-84 calculators, but some are unique to the TI-84 + C calculator.
- **Check Your Tech** examples help students understand that statistical calculations done by technology do not happen in a vacuum and assure them that they can get the same numerical values by hand. Although we place a higher value on interpreting results and verifying conditions required to apply statistical models, the numerical values are important, too.
- All **data sets** used in the exposition and exercises are available on the companion website at [www.pearsonglobaleditions.com/gould](http://www.pearsonglobaleditions.com/gould).

### *Guiding Students*


- Each chapter opens with a **Theme**. Beginners have difficulty seeing the forest for the trees, so we use a theme to give an overview of the chapter content.
- Each chapter begins by posing a real-world **Case Study**. At the end of the chapter, we show how techniques covered in the chapter helped solve the problem presented in the Case Study.
- **Margin Notes** draw attention to details that enhance student learning and reading comprehension.






The data icon appears alongside examples or discussions to indicate that the original data are available on the companion website.



**Caution** notes provide warnings about common mistakes or misconceptions.

 **Looking Back** reminders refer students to earlier coverage of a topic.


 **Details** clarify or expand on a concept.

-  **Key Points** highlight essential concepts to draw special attention to them. Understanding these concepts is essential for progress.
-  **Snapshots** break down key statistical concepts introduced in the chapter, quickly summarizing each concept or procedure and indicating when and how it should be used.
- An abundance of worked-out **examples** model solutions to real-world problems relevant to students' lives. Each example is tied to an end-of-chapter exercise so that students can practice solving a similar problem and test their understanding. Within the exercise sets, the icon **TRY** indicates which problems are tied to worked-out examples in that chapter, and the numbers of those examples are indicated.
- The **Chapter Review** that concludes each chapter provides a list of important new terms, student learning objectives, a summary of the concepts and methods discussed, and sources for data, articles, and graphics referred to in the chapter.

### Active Learning

- For each chapter we've included an activity, **Exploring Statistics**, that students are intended to do in class as a group. We have used these activities ourselves, and we have found that they greatly increase student understanding and keep students engaged in class.
- All exercises are located at the end of the chapter. **Section Exercises** are designed to begin with a few basic problems that strengthen recall and assess basic knowledge, followed by mid-level exercises that ask more complex, open-ended questions. **Chapter Review Exercises** provide a comprehensive review of material covered throughout the chapter.

The exercises emphasize good statistical practice by requiring students to verify conditions, make suitable use of graphics, find numerical values, and interpret their findings in writing. All exercises are paired so that students can check their work on the odd-numbered exercise and then tackle the corresponding even-numbered exercise. The answers to all odd-numbered exercises appear in the back of the text.

Challenging exercises, identified with an asterisk (\*), ask open-ended questions and sometimes require students to perform a complete statistical analysis. For exercises marked with a , accompanying data sets are available in MyStatLab and on the companion website.

- Most chapters include select exercises marked with a **g** within the exercise set, to indicate that problem-solving help is available in the **Guided Exercises** section. If students need support while doing homework, they can turn to the Guided Exercises to see a step-by-step approach to solving the problem.

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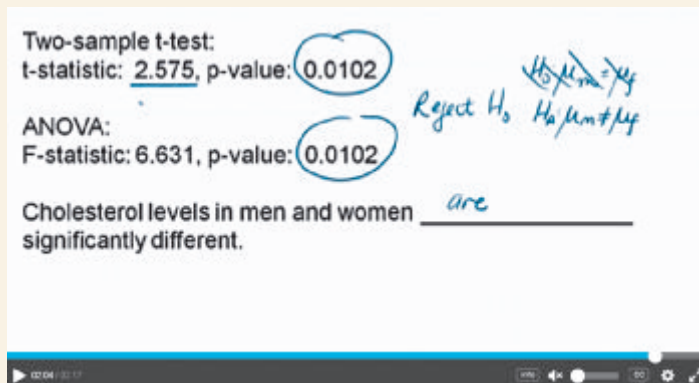
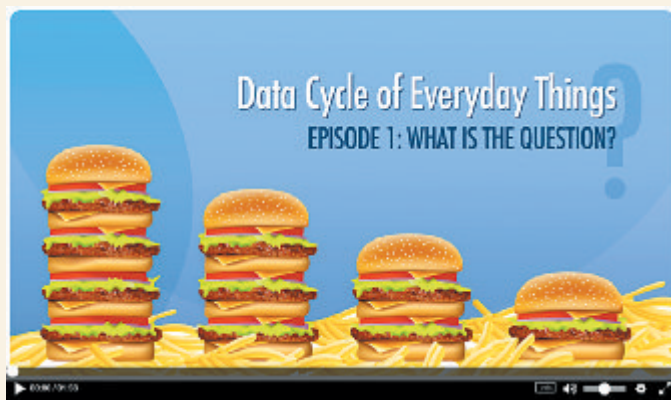
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**MyStatLab® Online Course** for *Essential Statistics: Exploring the World through Data*, Second Edition, Gould/Ryan/Wong (access code required)

MyStatLab is available to accompany Pearson’s market-leading text offerings. To give students a consistent tone, voice, and teaching method, each text’s flavor and approach is tightly integrated throughout the accompanying MyStatLab course, making learning the material as seamless as possible.

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*Data Cycle of Everyday Things Videos* demonstrate for students that data can be, and is, a part of everyday life! Through a series of fun and engaging episodes, students learn to collect, analyze, and apply data to answer any range of real-world statistical questions.

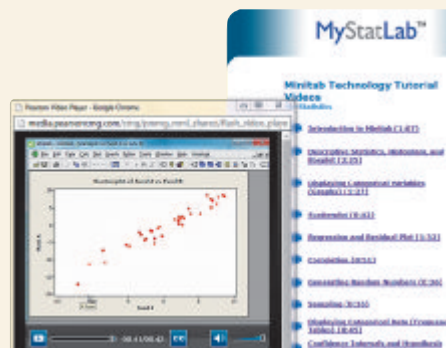


## Chapter Review Videos

*Chapter Review Videos* walk students through solving a selection of the more complex problems posed in each chapter, providing a review of the chapter’s key concepts and methods and offering students support where they most need it.

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*Technology Tutorials* provide brief video walkthroughs and step-by-step instructional study cards on common statistical procedures for Minitab®, Excel®, and the TI-83/84 graphing calculator.



# Resources for Success

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### PowerPoint Slides

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### Chapter Review Videos

**Chapter Review Videos** walk students through solving a selection of the more complex problems posed in each chapter, thereby offering a review of the chapter's key concepts and providing students support where they most need it.

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**The Data Cycle of Everyday Things Videos** demonstrate for students that data collection and data analysis can be applied to answer questions about everyday life. Through a series of fun and engaging episodes, students learn to collect, analyze, and apply data to answer any range of real-world statistical questions.

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# Essential Statistics: Exploring the World through Data

Second Edition

# 1

# Introduction to Data

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## THEME

Statistics is the science of data, so we must learn the types of data we will encounter and the methods for collecting data. The method used to collect data is very important because it determines what types of conclusions we can reach and, as you'll learn in later chapters, what types of analyses we can do. By organizing the data we've collected, we can often spot patterns that are not otherwise obvious.

This text will teach you to examine data to better understand the world around you. If you know how to sift data to find patterns, can communicate the results clearly, and understand whether you can generalize your results to other groups and contexts, you will be able to make better decisions, offer more convincing arguments, and learn things you did not know before. Data are everywhere, and making effective use of them is such a crucial task that one prominent economist has proclaimed statistics one of the most important professions of the decade (*McKinsley Quarterly* 2009).

The use of statistics to make decisions and convince others to take action is not new. Some statisticians date the current practice of statistics back to the mid-nineteenth century. One famous example occurred in 1854, when the British were fighting the Russians in the brutal Crimean War. A British newspaper had criticized the military medical facilities, and a young but well-connected nurse, Florence Nightingale, was appointed to study the situation and, if possible to improve it.

Nightingale carefully recorded the numbers of deaths, the causes of the deaths, and the times and dates

of the deaths. She organized these data graphically, and these graphs enabled her to see a very important pattern: A large percentage of deaths were due to contagious disease, and many deaths could be prevented by improving sanitary conditions. Within six months, Nightingale had reduced the death rate by half. Eventually she convinced Parliament and military authorities to completely reorganize the medical care they provided. Accordingly, she is credited with inventing modern hospital management.

In modern times, we have equally important questions to answer. Do cell phones cause brain tumors? Are alcoholic drinks healthful in moderation? Which diet works best for losing weight? What percentage of the public is concerned about job security? **Statistics**—the science (and art!) of collecting and analyzing observations to learn about ourselves, our surroundings, and our universe—helps answer questions such as these.

Data are the building blocks of statistics. This chapter introduces some of the basic types of data and explains how we collect them, store them, and organize them. These ideas and skills will provide a basic foundation for your study of the rest of the text.

## CASE STUDY

### Deadly Cell Phones?

In September 2002, Dr. Christopher Newman, a resident of Maryland, sued Motorola, Verizon, and other wireless carriers, accusing them of causing a cancerous brain tumor behind his right ear. As evidence, his lawyers cited a study by Dr. Lennart Hardell. Hardell had studied a large number of people with brain tumors and had found that a greater percentage of them used cell phones than of those who did not have brain tumors (CNN 2002; Brody 2002).

Speculation that cell phones might cause brain cancer began as early as 1993, when (as CNN reports) the interview show *Larry King Live* featured a man who claimed that his wife died because of cancer caused by her heavy cell phone use. However, more recent studies have contradicted Hardell's results, as well as earlier reports about the health risks of heavy cell phone use.

The judge in Dr. Newman's trial was asked to determine whether Hardell's study was compelling enough to support allowing the trial to proceed. Part of this



determination involved evaluating the method that Hardell used to collect data. If you were the judge, how would you rule? You will learn the judge's ruling at the end of the chapter. You will also see how the methods used to collect data about important *cause-and-effect relationships*—such as that which Dr. Newman alleged to exist between cell phone use and brain cancer—can affect the conclusions we can draw.

## SECTION 1.1

# What Are Data?

The study of statistics rests on two major concepts: variation and data. **Variation** is the more fundamental of these concepts. To illustrate this idea, draw a circle on a piece of paper. Now draw another one, and try to make it look just the same. Now another. Are all three exactly the same? We bet they're not. They might be slightly different sizes, for instance, or slightly different versions of round. This is an example of variation. How can you reduce this variation? Maybe you can get a penny and outline the penny. Try this three times. Does variation still appear? Probably it does, even if you need a magnifying glass to see, say, slight variations in the thickness of the penciled line.

**Data** are observations that you or someone else records. The drawings in Figure 1.1 are data that record our attempts to draw three circles that look the same. Analyzing pictorial data such as these is not easy, so we often try to quantify such observations—that is, to turn them into numbers. How would you measure whether these three circles are the same? Perhaps you would compare diameters or circumferences, or somehow try to measure how and where these circles depart from being perfect circles. Whatever technique you chose, these measurements could also be considered data.

Data are more than just numbers, though. David Moore, a well-known statistician, defined data as “numbers in context.” By this he meant that data consist not only of the numbers we record, but also of the story behind the numbers. For example,

10.00, 9.88, 9.81, 9.81, 9.75, 9.69, 9.5, 9.44, 9.31

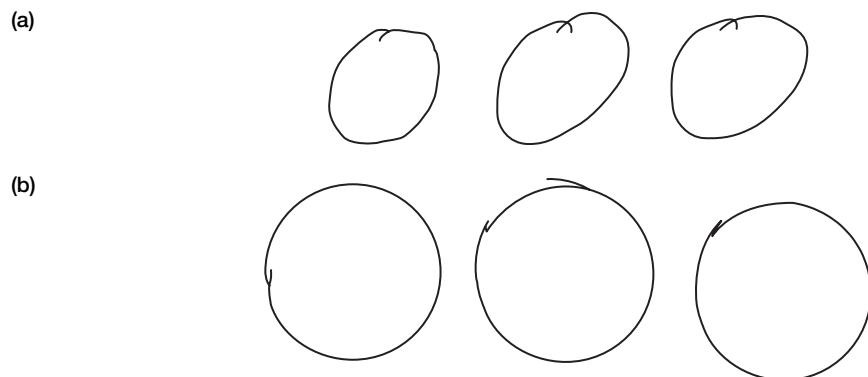
are just numbers. But in fact these numbers represent “Weight in pounds of the ten heaviest babies in a sample of babies born in North Carolina in 2004.” Now these numbers have a context and have been elevated into data. See how much more interesting data are than numbers?

### Details

#### Data Are What Data Is

If you want to be “old school” grammatically correct, then the word *data* is plural. So we say “data are” and not “data is.” The singular form is *datum*. However, this usage is changing over time, and some dictionaries now say that *data* can be used as both a singular and a plural noun.

► **FIGURE 1.1** (a) Three circles drawn by hand. (b) Three circles drawn using a coin. It is clear that the circles drawn by hand show more variability than the circles drawn with the aid of a coin.



These data were collected by the state of North Carolina in part to help researchers understand the factors that contribute to low-weight and premature births. If doctors understand the causes of premature birth, they can work to prevent it—perhaps by helping expectant mothers change their behavior, perhaps by medical intervention, and perhaps by a combination of both.

**KEY POINT**

Data are “numbers in context.”

In the last few years, our culture and economy have been inundated with data. The magazine *The Economist* has called this surge of data the “data deluge.” One reason for the rising tide of data is the application of automated data collection devices. These range from automatic sensors that simply record everything they see and store the data on a computer, to websites and smart phone apps that record every transaction their users make. Google, for example, saves every search you make and combines this with data on which links you click in order to improve the way it presents information (and also, of course, to determine which advertisements will appear on your search results).

Thanks to small, portable sensors, you can now join the “Personal Data Movement.” Members of this movement record data about their daily lives and analyze it in order to improve their health, to run faster, or just to make keepsakes—a modern-day scrapbook. Maybe you or a friend uses a Nike Fuel Band to keep track of regular runs. One of the authors of this text carries a FitBit in his pocket to record his daily activity. From this he learned that on days he lectures, he typically takes 7600 steps, and on days that he does not lecture, he typically only takes 4900 steps. Some websites, such as [your.floodingdata.com](http://your.floodingdata.com), make use of Twitter to help users collect, organize, and understand whatever personal data they choose to record.

Of course, it is not only machines that collect data. Humans still actively collect data with the intent of better understanding some phenomenon or making a discovery. Marketers prepare focus groups and surveys to describe the market for a new product. Sports analysts collect data to help their teams’ coaches win games, or to help fantasy football league players. Scientists perform experiments to test theories and to measure changes in the economy or the climate. In this text you’ll learn about the many ways in which data are used.

The point is that we have reached a historical moment where almost everything can be thought of as data. And once you find a way of capturing data about something in your world, you can organize, sort, visualize, and analyze those data to gain deeper understanding about the world around you.

## What Is Data Analysis?

In this text you will study the science of data. Most important, you will learn to analyze data. What does this mean? You are analyzing data when you examine data of some sort and explain what they tell us about the real world. In order to do this, you must first learn about the different types of data, how data are stored and structured, and how they are summarized. The process of summarizing data takes up a big part of this text; indeed, we could argue that the entire text is about summarizing data, either through creating a visualization of the data or distilling them down to a few numbers that we hope capture their essence.

**KEY POINT**

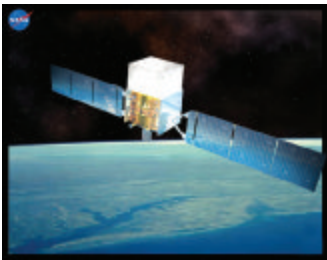
Data analysis involves creating summaries of data and explaining what these summaries tell us about the real world.

## SECTION 1.2

## Classifying and Storing Data



▲ FIGURE 1.2 A photo of Carhenge, Nebraska.



▲ FIGURE 1.3 Satellites in NASA's Earth Observing Mission record ultraviolet reflections and transmit these data back to Earth. Such data are used to construct images of our planet. Earth Observer (<http://eos.gsfc.nasa.gov>).

The first step in understanding data is to understand the different types of data you will encounter. As you've seen, data are numbers in context. But that's only part of the story; data are also recorded observations. Your photo from your vacation to Carhenge in Nebraska is data (Figure 1.2). The ultraviolet images streaming from the Earth Observer Satellite system are data (Figure 1.3). These are just two examples of data that are not numbers. Statisticians work hard to help us analyze complex data, such as images and sound files, just as easily as we study numbers. Most of the methods involve recoding the data into numbers. For example, your photos can be digitized in a scanner, converted into a very large set of numbers, and then analyzed. You might have a digital camera that gives you feedback about the quality of a photo you've taken. If so, your camera is not only collecting data but also analyzing it!

Almost always, our data sets will consist of characteristics of people or things (such as gender and weight). These characteristics are called **variables**. Variables are not “unknowns” like those you studied in algebra. We call these characteristics variables because they have variability: The values of the variable can be different from person to person.

## KEY POINT

Variables in statistics are different from variables in algebra. In statistics, variables record characteristics of people or things.

## Details

## More Grammar

We're using the word *sample* as a noun—it is an object, a collection of data that we study. Later we'll also use the word *sample* as a verb—that is, to describe an action. For example, we'll sample ice cream cones to measure their weight.

## Details

## Quantitative and Qualitative Data

Some statisticians use the word *quantitative* to refer to numerical variables (think “quantity”) and *qualitative* to refer to categorical variables (think “quality”). We prefer *numerical* and *categorical*. Both sets of terms are commonly used, and you should be prepared to hear and see both.

When we work with data, they are grouped into a collection, which we call either a **data set** or a **sample**. The word *sample* is important, because it implies that the data we see are just one part of a bigger picture. This “bigger picture” is called a **population**. Think of a population as the Data Set of Everything—it is the data set that contains all of the information about everyone or everything with respect to whatever variable we are studying. Quite often, the population is really what we want to learn about, and we learn about it by studying the data in our sample. However, many times it is enough just to understand and describe the sample. For example, you might collect data from students in your class simply because you want to know about the students in your class, and not because you wish to use this information to learn about all students at your school. Sometimes, data sets are so large that they effectively *are* the population, as you'll soon see in the data reflecting births in North Carolina.

## Two Types of Variables

The variables you'll find in your data set come in two basic types, which can themselves be broken into smaller divisions, as we'll discuss later.

**Numerical variables** describe quantities of the objects of interest. The values will be numbers. The weight of an infant is an example of a numerical variable.

**Categorical variables** describe qualities of the objects of interest. These values will be categories. The sex of an infant is an example of a categorical variable. The possible values are the categories “male” and “female.” Eye color of an infant is another example; the categories might be brown, blue, black, and so on. You can often identify categorical variables because their values are *usually* words, phrases, or letters. (We say “usually” because we sometimes use numbers to represent a word or phrase. Stay tuned.)